12	Centre of Examination :
QUESTION PAPER	Roll No. :
SERIES CODE	Name of Candidate :
A	C A II

## Entrance Test for Ph.D. (Computer Science)

# [ 2013 ]

Time : 3 hours

Maximum Marks: 70

### INSTRUCTIONS FOR CANDIDATES

Candidates must carefully read the following instructions before attempting the Question Paper :

- (i) Write your Name and Roll Number in the space provided for the purpose on the top of this Question Paper and in the OMR/Answer Sheet.
- (ii) This Question Paper has Two Parts : Part-A and Part-B.
- (iii) Part—A (Objective-type) has 30 questions of **1** mark each. All questions are compulsory.
- (iv) Part—B (Objective-type) has 40 questions of **1** mark each. All questions are compulsory.
- (v) Symbols have their usual meanings.
- (vi) Please darken the appropriate Circle of 'Question Paper Series Code' on the OMR Sheet in the space provided.
- (vii) Questions of both the parts should be answered on OMR Sheet.
- (viii) Answers written by the candidates inside the Question Paper will NOT be evaluated.
- (ix) Calculators and Log Tables may be used.
- (x) Pages at the end have been provided for Rough Work.
- (xi) **Return the Question Paper and the OMR Sheet** to the Invigilator at the end of the Entrance Test.
- (xii) DO NOT FOLD THE OMR SHEET.

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## INSTRUCTIONS FOR MARKING ANSWERS IN THE 'OMR SHEET'

- 1. Please ensure that you have darkened the appropriate Circle of 'Question Paper Series Code' on the OMR Sheet in the space provided.
- 2. Use only Blue/Black Ballpoint Pen to darken the Circle. Do not use Pencil, to darken the Circle for Final Answer.
- 3. Please darken the whole Circle.
- 4. Darken ONLY ONE CIRCLE for each question as shown below in the example.

### Example :



- 5. Once marked, no change in the answer is allowed.
- 6. Please do not make any stray marks on the OMR Sheet.
- 7. Please do not do any rough work on the OMR Sheet.
- 8. Mark your answer only in the appropriate Circle against the number corresponding to the question.
- 9. There will be no negative marking in evaluation.

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### PART—A

1. If  $L = \{(x, y) | y = e^x, x \in R\}$  and  $M = \{(x, y) | y^2 = x, x \in R\}$ , then

- (a)  $M \subseteq L$
- (b)  $L \subseteq M$
- (c)  $L \cap M = \phi$
- (d)  $L \cup M = L$
- 2. Which of the following statements is the negation of the statement '4 is even or -5 is negative'?
  - (a) 4 is odd and -5 is not negative
  - (b) 4 is even or -5 is not negative
  - (c) 4 is odd or -5 is not negative
  - (d) 4 is even and -5 is not negative
- 3. A box contains 2 white balls, 3 black balls and 4 red balls. In how many ways can 3 balls be drawn from the box, if at least one black ball is to be included in the draw?
  - (a) 40
  - (b) 45
  - (c) 96
  - (d) 64
- 4. The probability of solving a question by three students are  $\frac{1}{2}$ ,  $\frac{1}{4}$  and  $\frac{1}{6}$  respectively. Probability of question being solved will be
  - (a)  $\frac{31}{48}$
  - (b)  $\frac{33}{48}$
  - (c)  $\frac{35}{48}$
  - (d)  $\frac{37}{48}$

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5. The mean and variance of a binomial distribution are 4 and 3 respectively. Then the probability of getting exactly six successes in this distribution is

(a) 
$${}^{16}C_6\left(\frac{1}{4}\right)^6\left(\frac{3}{4}\right)^{10}$$
  
(b)  ${}^{16}C_6\left(\frac{1}{4}\right)^{16}\left(\frac{3}{4}\right)^{20}$   
(c)  ${}^{16}C_6\left(\frac{1}{4}\right)^8\left(\frac{3}{4}\right)^{12}$   
(d)  ${}^{16}C_6\left(\frac{1}{4}\right)^{12}\left(\frac{3}{4}\right)^{16}$ 

6. One in five of the general population are left-handed. The probability that of four randomly selected people, three becoming left-handed is approximately

- (a) 0.200
- (b) 0.600
- (c) 0.037
- (d) 0.026

7.	$\lim_{n\to\circ}$	$ \frac{1^2 + 2^2 + n^3}{n^3} $	$\cdots + n^2$	will be
	(a)	1		
	(b)	-1		
	(c)	$\frac{1}{2}$		
	(d)	$\frac{1}{3}$		

8. The maximum value of  $\frac{\log x}{x}$  will be

(a) e(b)  $e^{\frac{1}{e}}$ (c)  $\frac{1}{e}$ 

(d)  $e^2$ 

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9. The value of  $\int \frac{dx}{1+e^x}$  is (a)  $\frac{e^x}{1+e^x} + c$ (b)  $\log\left(\frac{e^x}{1+e^x}\right) + c$ (c)  $\log(1+e^x) + c$ 

(d) 
$$\log e^x + c$$

**10.** The particular integral of  $\frac{d^2y}{dx^2} + y = \cos x$  is

(a)  $\frac{x \sin x}{2}$ (b)  $\frac{x \cos x}{2}$ (c)  $\frac{xe^{x}}{2}$ (d)  $\frac{x \tan x}{2}$ 

**11.** The integrating factor of  $(x^2 + y^2) dx = 2xydy$  is

(a)  $\frac{-1}{x^2}$ (b)  $\frac{1}{x^2}$ (c)  $\frac{-1}{x}$ (d)  $\frac{1}{x}$ 

12. What will be the equation of tangent to parabola  $y^2 = 7x$ , which is parallel to straight line 4y - x + 3 = 0?

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- (a) 4y x + 28 = 0
- (b) x 4y + 14 = 0
- (c) 4y x + 14 = 0
- (d) x 4y + 28 = 0

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**13.** The perpendicular distance between the lines 3x + 4y + 7 = 0 and 3x + 4y - 3 = 0 will be

- (a) 4
- (b) 3
- (c) 2
- (d) 1

14. What will be the equation of circle whose equations of diameters are x + y = 6 and x + 2y = 4 and its radius is 10?

- (a)  $x^2 + y^2 + 16x + 12y 5 = 0$
- (b)  $x^2 + y^2 + 13x 11y 8 = 0$
- (c)  $x^2 + y^2 + 7x 5y + 6 = 0$
- (d)  $x^2 + y^2 16x + 4y 32 = 0$

**15.** The angle between the vectors  $\vec{a} = 3\hat{i} - 2\hat{j} + \hat{k}$  and  $\vec{b} = 2\hat{i} + \hat{j} + 3\hat{k}$  is

- (a) 75°
- (b) 60°
- (c) 45°
- (d) 30°

16.  $\hat{i} \cdot (\hat{j} \times \hat{k}) + \hat{j} \cdot (\hat{i} \times \hat{k}) + \hat{k} \cdot (\hat{i} \times \hat{j})$  is equal to

- (a) 3
- (b) -3
- (c) 0
- (d) 1

17. If  $M = [a_{ij}]_{m \times n}$  be a matrix such that  $a_{ij} = 1$  for all *i* and *j*, then

- (a) rank (M) = m
- (b) rank (M) = n
- (c) rank (M) > 1
- (d) rank (M) = 1

**18.** If  $a \neq b \neq c$ , then the value of x satisfying the equation det  $\begin{bmatrix} 0 & x-a & x-b \\ x+a & 0 & x-c \\ x+b & x+c & 0 \end{bmatrix} = 0$  is

- (a) a
- (b) *b*
- (c) *c*
- (d) 0

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19. What is the output of the following program?
                #include <stdio.h>
               void main()
               {
                       int i, j, k;
               i=2;
               j=4;
               k=i++>j&2;
               if(++k & ++i < --j||i++)
               {
                  j=++k;
               }
               printf("%d %d %d",i,-j--,k);
               getchar()
               }
     (a) 4-3 2
                                          (b) 5-3 2
                                          (d) 5-2 2
          4-22
      (c)
20. What is the output of the following program?
                #include <stdio.h>
               void main()
               {
               int i=0;
                for(i=0;i<20;i++)
                {
                     switch(i)
                     {
                     case 0:
                     i+=5;
                     case 1:
                     i+=2;
                     case 5:
                     i+=5;
                     default:
                     i+=4;
                      break;
                      }
                      printf("%d", i);
                }
                getchar();
                }
                                           (b) 4 2
           4 4
      (a)
                                           (d) 16 21
           5 20
      (c)
```

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```
What is the output of the following program?
21.
                      #include <stdio.h>
                      #include <string.h>
              void main()
              {
              char s1[10]="abcd";
              char s2[10];
              char s3[10]="efgh";
              int i;
              i=strcmp(strcat(s3,strcpy(s2,s1)),strcat(s3,"abcd"));
              printf("%d",i);
              getch();
              }
           0
      (a)
      (b)
           -1
      (c)
            1
            2
      (d)
      How many times the pattern "South Asian University" will get printed?
22.
                void main()
                 {
                 int x;
                 for(x=-1; x<=10; x++)
                 {
                   if(x<5)
                     continue;
                   else
                      break;
                   printf("South Asian University");
                 }
                 }
            Infinite times
       (a)
            0 times
       (b)
            11 times
       (c)
             6 times
       (d)
```

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23. Consider the following recursive function : int fun (int n)

{
 If (n = = 4)
 return 2;
 else
 return 2 \* fun (n + 1);
}

What is the value returned by the function call fun (2)?

- (a) 2
- (b) 4
- (c) 8
- (d) 16

24. Which of the following cannot be checked in a switch-case statement?

- (a) enum
- (b) float
- (c) int
- (d) char

25. The memory address of the first element of an array is called

- (a) floor address
- (b) foundation address
- (c) first address
- (d) base address
- **26.** If a signal passing through a gate is inhibited by sending a LOW into one of the inputs, and the output is HIGH, the gate is
  - (a) AND
  - (b) NAND
  - (c) NOR
  - (d) OR

**27.** Simplified form of the Boolean expression (X + Y + XY)(X + Z) is

- (a) X+Y+Z
- (b) XY + YZ
- (c) X + YZ
- (d) XZ + Y

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$\checkmark$	WX			
ΥZ	00	01	11	10
00	1	1	1	
01				
11		1	1	
10	1		1	1

- (a) F(w, x, y, z) = x'z'
- (b) F(w, x, y, z) = (x' + z') + (w + z')(x + y + z)
- (c) F(w, x, y, z) = xz + w'z + x'y'z'
- (d) F(w, x, y, z) = x'z' + wz'wz' + xyz

29. The minimum number of D flip-flops needed to design a mod-150 counter is

- (a) 128
- (b) 7
- (c) 8
- (d) 150

30.

What is the Boolean expression for the circuit given below?



- (a) F(A, B) = A'B + A'B'
- (b)  $F(A, B) = A \oplus B$
- (c) F(A, B) = A' + B'
- (d)  ${}^{\circ}F(A, B) = A'B'$

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- 31. Time taken for addition of element in queue is
  - (a) O(l)
  - (b) *O*(*n*)
  - (c)  $O(\log n)$
  - (d) None of the above
- **32.** When inorder traversing a tree resulted *EACKFHDBG*. The preorder traversal would return
  - (a) FAEKCDBHG
  - (b) FAEKCDHGB
  - (c) EAFKHDCBG
  - (d) FEAKDCHBG

**33.** If every node u in G is adjacent to every other node v in G, a graph is said to be

- (a) isolated
- (b) complete
- (c) finite
- (d) strongly connected
- **34.** A hash function f defined as f (key) = key mod 7, with linear probing, inserts the keys 37, 38, 72, 48, 98, 11, 56 into a table. Then 11 will be stored in the location
  - (a) 3
  - (b) 4
  - (c) 5
  - (d) 6

**35.** A *B*-tree of order m has maximum of —— children.

- (a) m
- (b) m+1
- (c) *m* 1
- (d) m/2

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The complexity of merge sort algorithm is

(a)	O(n)	(b)	$O(\log n)$

(c)  $O(n^2)$  (d)  $O(n\log n)$ 

**37.** A graph with every node u connected with every other node v is a

- i. bipartite graph
- ii. connected graph
- iii. complete graph

Choose the correct statement(s) from the above.

(a) only i

- (b) Both i and ii
- (c) Both ii and iii
- (d) All i, ii and iii
- **38.** Which of the given options provides the increasing order of asymptotic complexity of functions  $f_1$ ,  $f_2$ ,  $f_3$  and  $f_4$  for n > 2?
  - $f_{1}(n) = 2^{n}$   $f_{2}(n) = n^{\frac{1}{2}}$   $f_{3}(n) = n \log n$   $f_{4}(n) = n^{\log n}$ (a)  $f_{3}, f_{2}, f_{4}, f_{1}$ (b)  $f_{3}, f_{2}, f_{1}, f_{4}$ (c)  $f_{2}, f_{3}, f_{1}, f_{4}$ (d)  $f_{2}, f_{3}, f_{4}, f_{1}$
- **39.** Let P be a shortest path from some vertex s to some other vertex t in a graph. If the weight of each edge in the graph is increased by one
  - (a) P will still be a shortest path from s to t
  - (b) P may or may not be a shortest path from s to t
  - (c) P will never be a shortest path from s to t

(d) None of the above

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40. Consider the following two functions :

$$f(n) = n^{3}, \text{ if } 0 \le n < 10000$$
  
=  $n^{2}, \text{ if } n \ge 10000$   
 $g(n) = n, \text{ if } 0 \le n < 100$   
=  $n^{2} + 5n, \text{ if } n \ge 100$ 

Which of the following is true?

- (a) f(n) is of  $O(n^3)$
- (b) g(n) is O(n)
- (c) O(f(n)) is same as O(g(n))
- (d) None of the above

**41.**  $\sum_{k=1}^{n} O(n^2)$ , where O(n) stands for order of n, is

- (a)  $O(n^2 \log n)$
- (b)  $O(n^2)$
- (c)  $O(n^3)$
- (d) None of the above

42. The strongly connected components of the graph



are

- (a)  $\{\{ABDGCEF\}, \{H\}\}$
- (b)  $\{\{ABCE\}, \{DG\}, \{FH\}\}$
- (c)  $\{\{ABC\}, \{DG\}, \{EF\}, \{H\}\}$
- (d) None of the above
- **43.** Which of the following is the Huffman code for the characters  $\{a, b, c, d, e, f\}$  having the following frequencies?

с	a	b	с	d	е	f
f (c)	45	13	12	16	9	5

- (a) 0, 101, 100, 111, 1101, 1100
- (b) 0, 10, 110, 1110, 11110, 11111
- (c) 11, 10, 01, 001, 0001, 0000
- (d) 11, 10, 011, 010, 001, 000

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44. Measurements of a certain system have shown that the average process runs for a time T before blocking for I/O. A process switch requires time S, which is effectively waste (overhead). Consider a round-robin scheduler with quantum Q. Assuming there is no variation among the processes, if Q < T, then the CPU efficiency is

- (a) T/(S+T)
- (b) T/(T + S[T/Q])
- (c) Q/(Q+S)
- (d) 0.5
- **45.** An 'aging algorithm' is being used to estimate the mean value of a sequence of observations  $X_n$ . Suppose that the distribution of the  $X_n$ 's does not actually vary over time, so that they are independent random variables, identically distributed with mean  $\mu$  and variance  $\sigma^2$ . Let  $Y_n$  be the *n*th estimate computed by the aging algorithm, so  $Y_n = \alpha X_n + (1-\alpha)Y_{n-1}$  for large *n*. Then, the expected value of  $Y_n$  and the variance of  $Y_n$  are
  - (a)  $\mu$  and  $\sigma^2 \alpha / (2 \alpha)$
  - (b)  $\mu$  and  $\sigma^2 \alpha / (1 \alpha)$
  - (c)  $\mu$  and  $\sigma^2$
  - (d)  $\mu$  and  $\sigma^2 \alpha^2$
- **46.** A batch-processing system needs a module to manage allocation of N line printers, identified by integers in the range 0 up to N-1. It must provide functions AllocPrinter and FreePrinter. Which of the following is a reasonable requirement?
  - (a) AllocPrinter allocates a printer and returns its number. Printers can be allocated to any client, since it is very unlikely that two clients will request the same printer at the same instant
  - (b) AllocPrinter allocates a printer and returns its number; this printer is not allocated to any other client for some fixed period of time, after which the number is passed to *FreePrinter*
  - (c) AllocPrinter allocates a printer and returns its number; this printer is not allocated to any other client until the same number is passed as an argument to FreePrinter
  - (d) AllocPrinter simply allocates a printer, FreePrinter simply frees a printer
- 47. The message passing scheme for synchronization can be used only if the processes are
  - (a) not aware of each other
  - (b) indirectly aware of each other
  - (c) directly aware of each other
  - (d) None of the above

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- 48. The CPU scheduling parameter throughput refers to
  - (a) keeping CPU as busy as possible
  - (b) total time spent by processes in waiting state
  - (c) amount of time it takes for processes to start responding
  - (d) number of processes completed per unit time
- 49. If the baud rate is 400 for a 4-phase-shift keying (4-PSK) signal, the bit rate is
  - (a) 100 bps
  - (b) 400 bps
  - (c) 800 bps
  - (d) 1600 bps
- 50. If we want to combine 20 voice-grade signals (each with 4 kHz) with a guard band of 1 kHz between them to prevent interference, how much bandwidth do we need (in kHz)?
  - (a) 81
  - (b) 101
  - (c) 99
  - (d) 100
- **51.** In the CSMA/CD protocol, what condition on the transmission delay  $T_{\text{trans}}$  and the propagation delay  $T_{\text{prop}}$  has to be satisfied to guarantee that a node always detects a collision?
  - (a)  $T_{\text{trans}} > T_{\text{prop}}$
  - (b)  $T_{\text{trans}} > 2T_{\text{prop}}$
  - (c)  $T_{\text{trans}} < T_{\text{prop}}$
  - (d)  $2T_{\text{trans}} < T_{\text{prop}}$

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**52.** If a class *B* network on the Internet has a subnet mask of 255.255.248.0, what is the maximum number of hosts per submet?

- (a) 1022
- (b) 1023
- (c) 2046
- (d) 2047
- **53.** Host A sends a TCP segment (Seq = 43, ACK = 103), to which host B replies with a TCP segment (Seq = 103, ACK = 57). The payload of the first TCP segment is
  - (a) 14 bytes long
  - (b) 43 bytes long
  - (c) 46 bytes long
  - (d) 57 bytes long

54. What is the minimum Hamming distance for the following set of four 6-bit code words?

	000000	000111	111000	111111
2				

(b) 3

(a)

- (c) 4
- (d) 5

55. ICMP (Internet Control Message Protocol) is used by

- (a) ping to provide echo request/reply
- (b) traceroute to measure the delay between the routers from a source to a destination
- (c) host and routers to communicate network level information
- (d) All of the above

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- 56. You want to check if there is an assignment of TRUE and FALSE values to N = 100Boolean variables that makes a formula F true. If a computer can check the truth value of F for any particular assignment in 1 picosecond ( $10^{-12}$  seconds), approximately how long will it take in the worst case to determine that there is no assignment of values to the N variables that can make formula F true?
  - (a)  $100 \times 10^{-12}$  seconds
  - (b) 10 seconds
  - (c)  $10^8$  seconds
  - (d)  $10^{18}$  seconds
- 57. The dataflow diagram
  - i. depicts relationships between data objects
  - ii. depicts functions that transform the data flow
  - iii. indicates how data are transformed by the system
  - iv. indicates system reactions to external events

Choose the correct statement(s) from the above.

- (a) i, ii
- (b) ii, iii
- (c) i
- (d) None of the above

58. Software deteriorates rather than wears out, because

- i. software suffers from exposure to hostile environments
- ii. defects are more likely to arise after software has been used often
- iii. multiple change requests introduce errors in component interactions

iv. software spare parts become harder to order

Choose the correct statement(s) from the above.

- (a) i
- (b) ii, iii
- (c) iii
- (d) None of the above

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### 59. The state transition diagram

- i. depicts relationships between data objects
- ii. depicts functions that transform the data flow
- iii. indicates how data are transformed by the system

iv. indicates system reactions to external events Choose the correct statement(s) from the above.

- (a) i
- (b) ii, iii
- (c) iv
- (d) None of the above

60. A relation is in Boyce-Codd Normal Form (BCNF) if every

- (a) determinant is a candidate key
- (b) key is atomic
- (c) attribute is fully functional dependent on primary key
- (d) attribute is independent on primary key

61. Indexes in DBMS are used to

- (a) organize records and speedup retrieval
- (b) speedup sorting of files
- (c) sort the selected records on the desired attribute
- (d) speedup joining of tables on selected attributes

62. Referential integrity dictates that the value of a

- (a) primary key must appear in a foreign key of the related table
- (b) foreign key must appear in a primary key of the related table
- (c) primary key cannot appear in a foreign key of the related table
- (d) foreign key cannot appear in a primary key of the related table

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- **63.** If r(A, C) and s(A, D) are any relations with the given attributes, then which of the following relational algebra expressions means the join of R and S?
  - (a)  $\pi_{A,C,D}(\sigma_{r\cdot A=s\cdot A}(r\times s))$
  - (b)  $\pi_{A,C,D}(\sigma_{s\cdot A=r\cdot A}(r\times s))$
  - (c)  $\sigma_{A,C,D}(\pi_{r\cdot A=s\cdot A}(r\times s))$
  - (d) None of the above

64. Which of the following is not a characteristic of metadata?

- (a) Includes user data
- (b) Data that describes user data
- (c) Stored in data dictionary
- (d) Used while execution of DML commands
- 65. Which of the following is true about database transactions?
  - i. Execution of a transaction should be atomic
  - ii. Effects of a transaction persist even if the system crashes before it can be completed
  - iii. A transaction is either committed or aborted
  - iv. A transaction is sequence of logically related actions

Choose the correct statement(s) from the above.

- (a) i, ii, iv
- (b) i, ii, iii
- (c) i, iii, iv
- (d) All of the above

66. The most common addressing technique employed by a CPU is

- (a) immediate
- (b) direct
- (c) indirect
- (d) All of the above

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**67.** Which of the following registers is used to keep track of address of the memory location where the next instruction is located?

- (a) Memory address register
- (b) Memory data register
- (c) Instruction register
- (d) Program counter register
- **68.** The number of instructions needed to add n numbers and store the result in memory using only one address instructions is
  - (a) n
  - (b) n+1
  - (c) n-1
  - (d) independent of n
- **69.** Which of the following need not necessarily be saved on a context switch between processes?
  - (a) General purpose register
  - (b) Translation look aside buffer
  - (c) Program counter
  - (d) All of the above

70. The sequence of events that happen during a typical fetch operation is

- (a) PC > MAR > Memory > MDR > IR
- (b) PC > Memory > MAR > IR > MDR
- (c) PC > IR > Memory
- (d) Memory > PC > MAR > IR > MDR

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